

## Range of Possible Collisions

Total Splat!  
(Stick)

The  
Perfect  
Bounce

**Completely**

**Completely**

**Inelastic**

.....less bounce

more bounce .....

**Elastic**

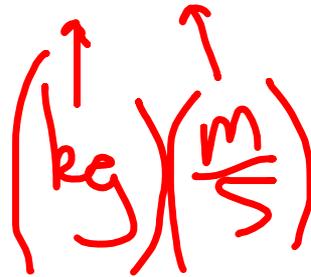


← - - More Inelastic

More Elastic - - →

# Momentum

$$\mathbf{p} = \mathbf{m} \mathbf{v}$$



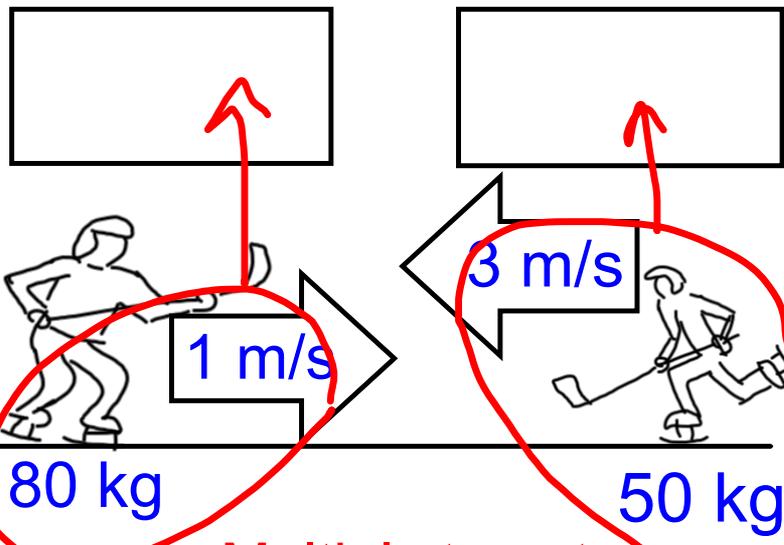
Handwritten red annotations for the equation  $\mathbf{p} = \mathbf{m} \mathbf{v}$ . The units are shown as  $(\text{kg})$  for mass and  $(\frac{\text{m}}{\text{s}})$  for velocity, with red arrows pointing upwards from each unit.

If velocity is left, it's negative!

### Calculating Total Momentum Before a Collision

**total**  
**momentum**

LEFT = NEGATIVE



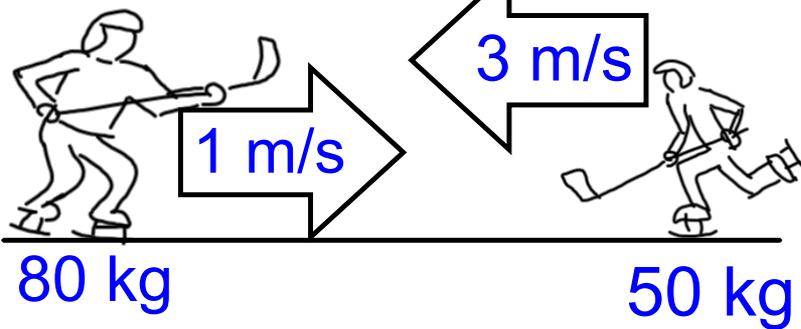
- After collision:
- Goes left
  - Goes right
  - Stops

Multiply to get momentum

### Calculating Total Momentum Before a Collision

LEFT = NEGATIVE

total  
momentum



After collision:

- Goes left
- Goes right
- Stops

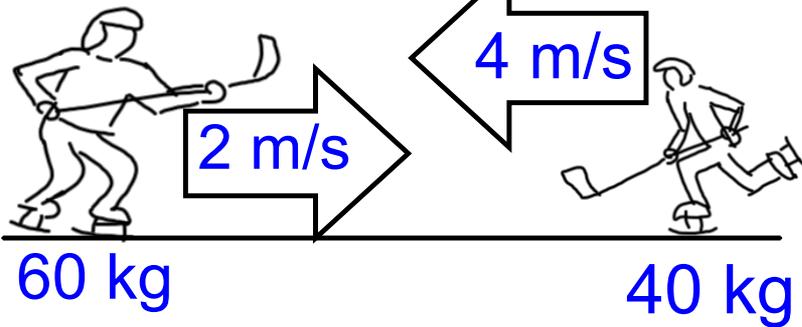
Goes left because the total momentum is negative.

### Calculating Total Momentum Before a Collision

total  
momentum

LEFT = NEGATIVE

- After collision:
- Goes left
  - Goes right



**Calculating Total Momentum Before a Collision****total  
momentum**

$$-40 \text{ kg m/s}$$

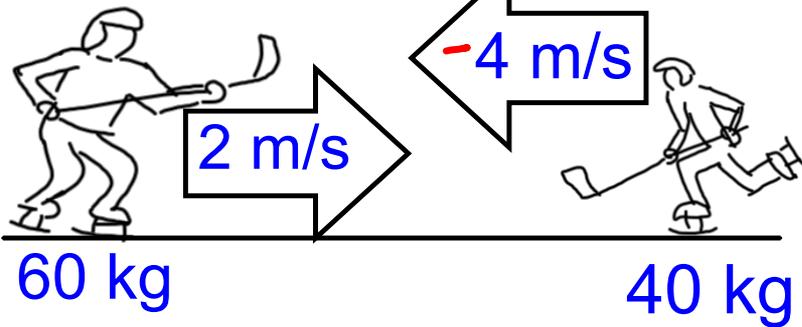
LEFT = NEGATIVE

$$120 \text{ kg m/s}$$

$$-160 \text{ kg m/s}$$

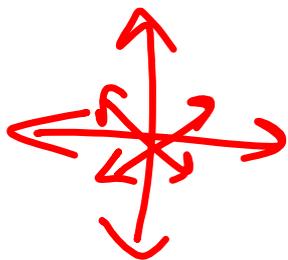
After collision:

- Goes left
- Goes right

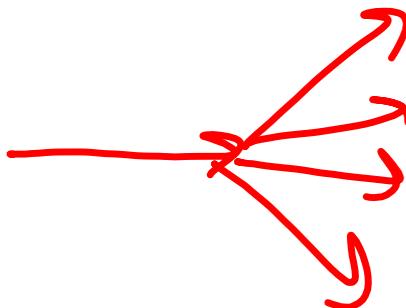


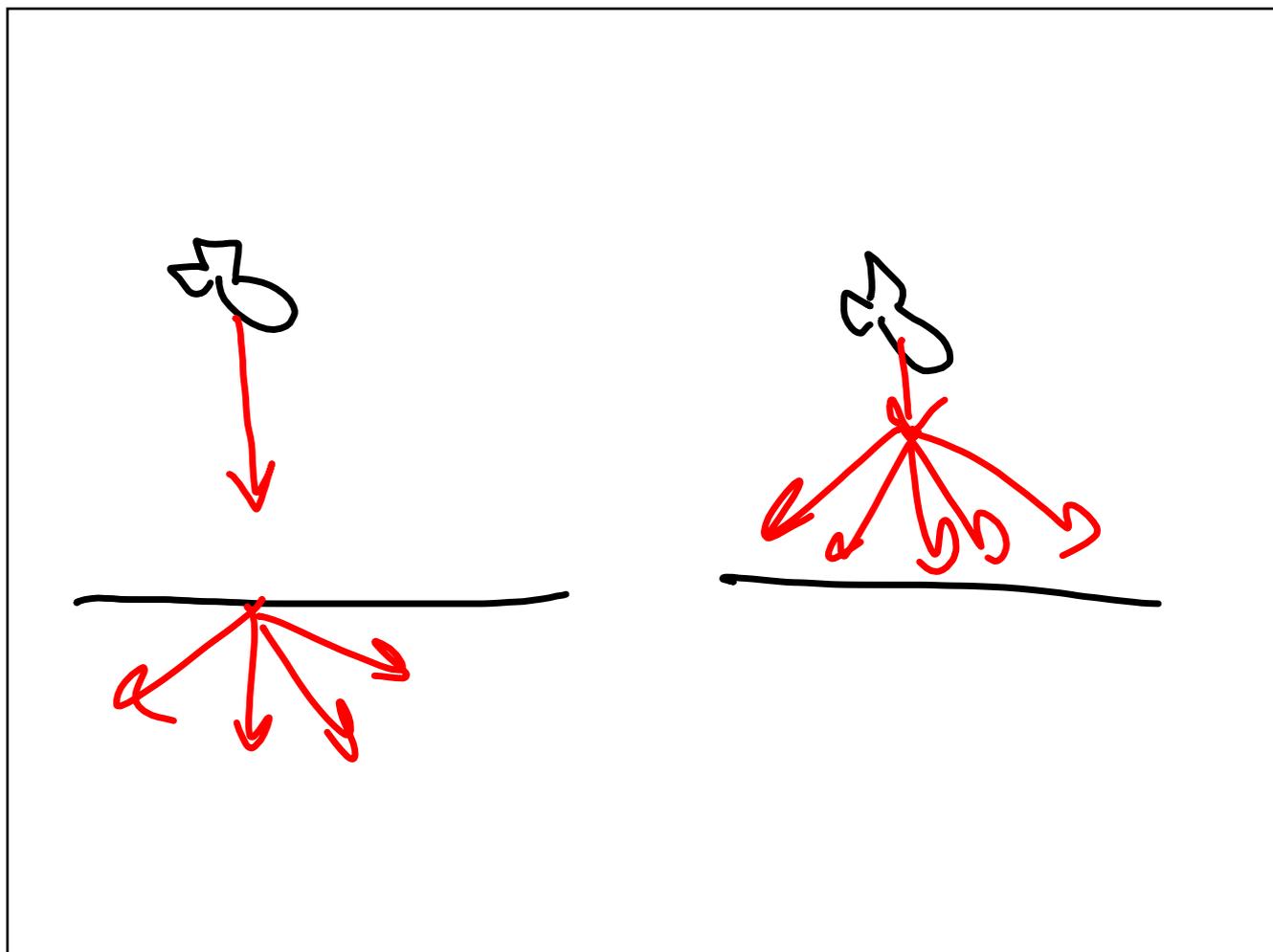
# Explosions

If they start with  
**NO** momentum

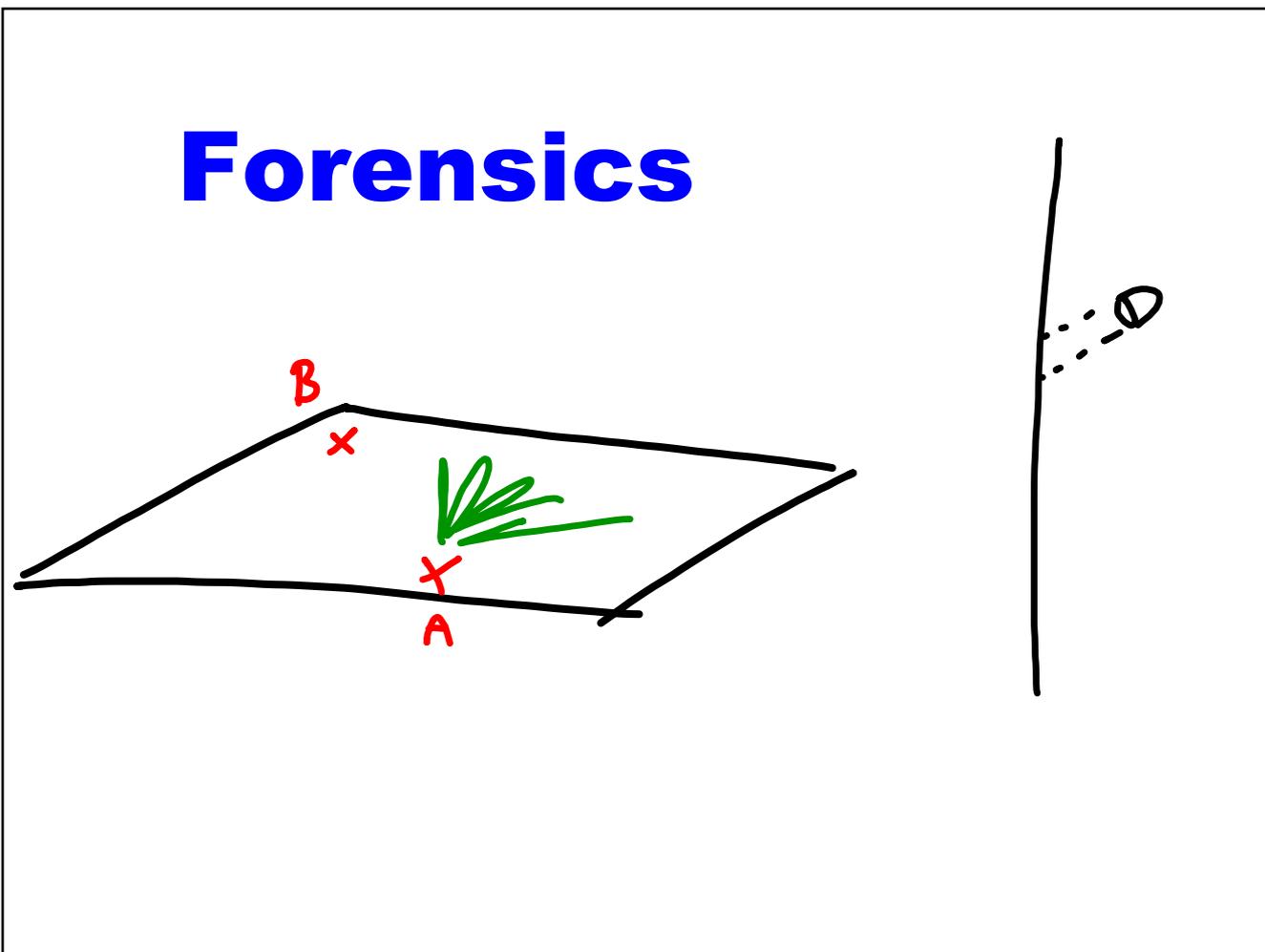


If they start with  
**SOME** momentum





# Forensics



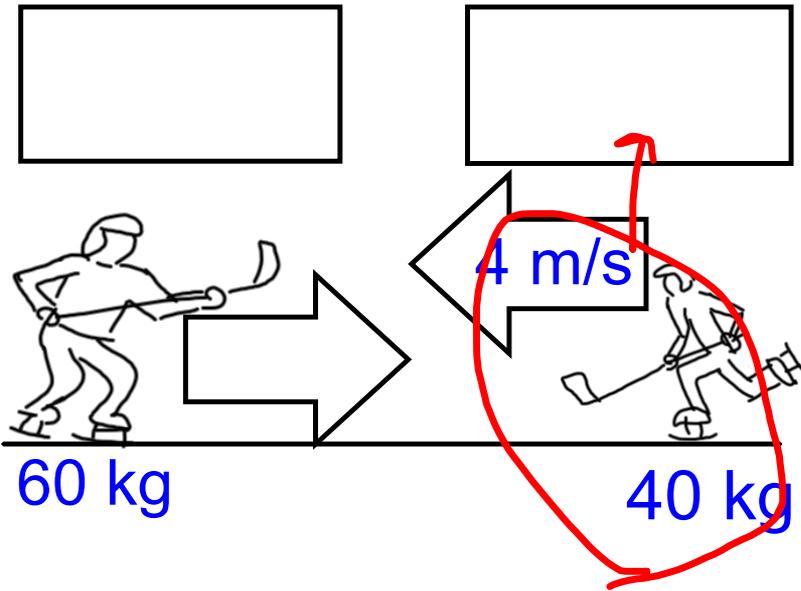
### Calculating Total Momentum Before a Collision

**total  
momentum**

**-40 kgm/s**

**LEFT = NEGATIVE**

After collision:  
 Goes left  
 Goes right



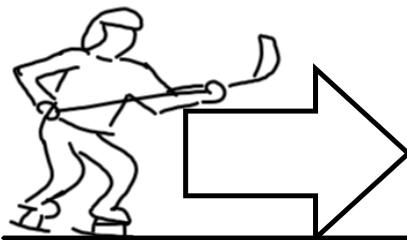
Multiply. Then that momentum plus the unknown momentum must make the total.

### Calculating Total Momentum Before a Collision

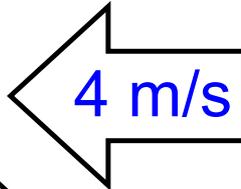
**total  
momentum**

**-40 kgm/s**

**LEFT = NEGATIVE**



**60 kg**



**40 kg**

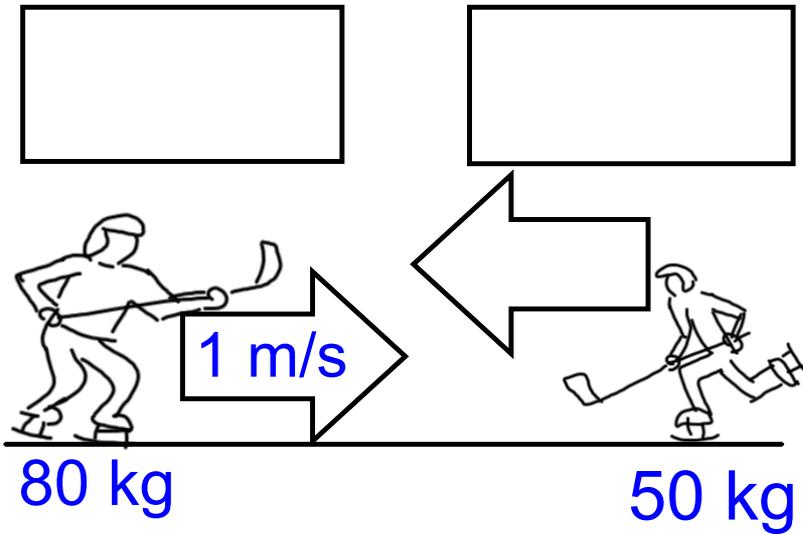
After collision:

- Goes left
  - Goes right
- call the unknown momentum  $x$ .

Then divide to get the velocity.

**Calculating Total Momentum Before a Collision**

**total  
momentum** **-70 kgm/s**

**LEFT = NEGATIVE**

After collision:

- Goes left
- Goes right
- Stops

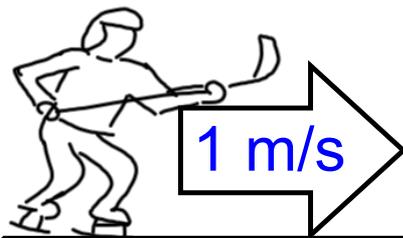
### Calculating Total Momentum Before a Collision

LEFT = NEGATIVE

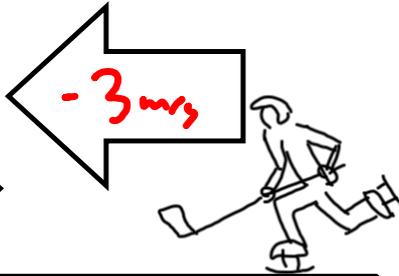
total momentum  $-70 \text{ kgm/s}$

$80 \text{ kgm/s}$

$X = -150 \text{ kgm/s}$



80 kg



50 kg

After collision:

- Goes left
- Goes right
- Stops

$$X + 80 = -70$$
$$-80 \quad -80$$
$$X = -150 \text{ kgm/s}$$

## Kinetic Energy

$$\left(\frac{m}{2}\right)v^2$$

Predicts

How hard it is to stop.

Damage it can do.

Speed at the bottom of a hill

## Momentum



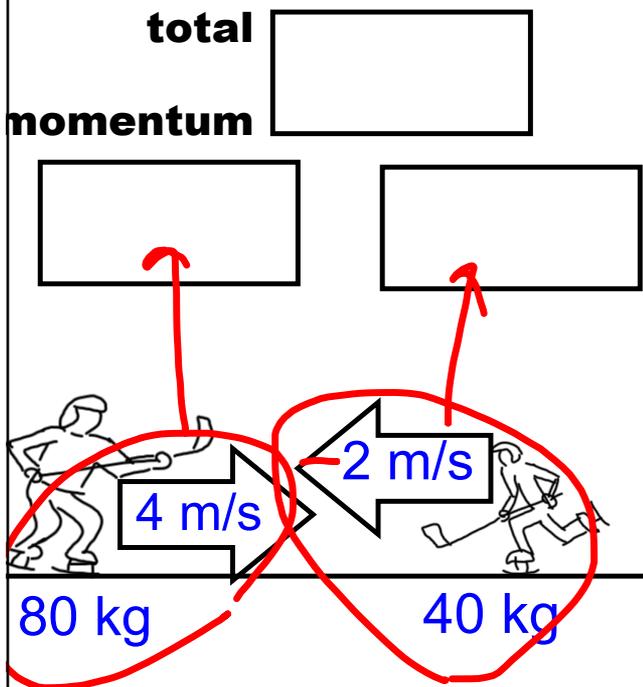
## **The Law of Conservation of Momentum**

**Total Momentum**  
**BEFORE a Collision** = **Total Momentum**  
**AFTER a Collision**

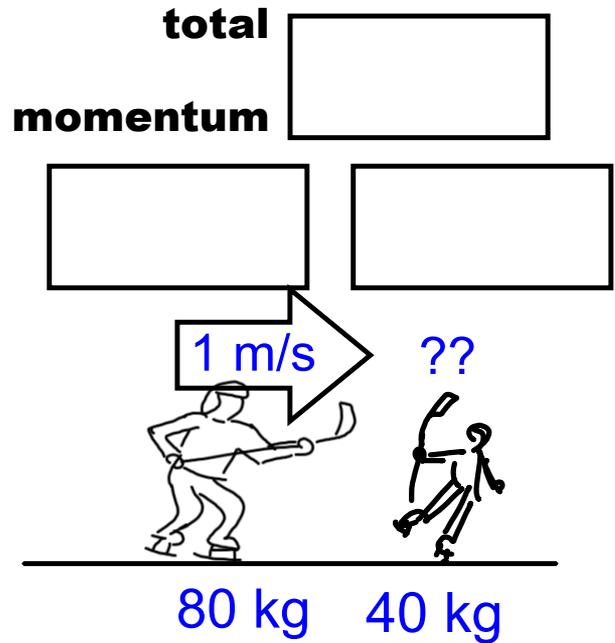
(If there are no outside forces)

### Calculating Total Momentum Before a Collision

LEFT = NEGATIVE



Find the total momentum just like you've done.



The total after has to be the same.

### Calculating Total Momentum Before a Collision

LEFT = NEGATIVE

total momentum  $240 \text{ kg}\cdot\text{m/s}$

$320 \text{ kg}\cdot\text{m/s}$

$-80 \text{ kg}\cdot\text{m/s}$

80 kg                      40 kg

total momentum  $240 \text{ kg}\cdot\text{m/s}$

SAME

$80 \text{ kg}\cdot\text{m/s}$

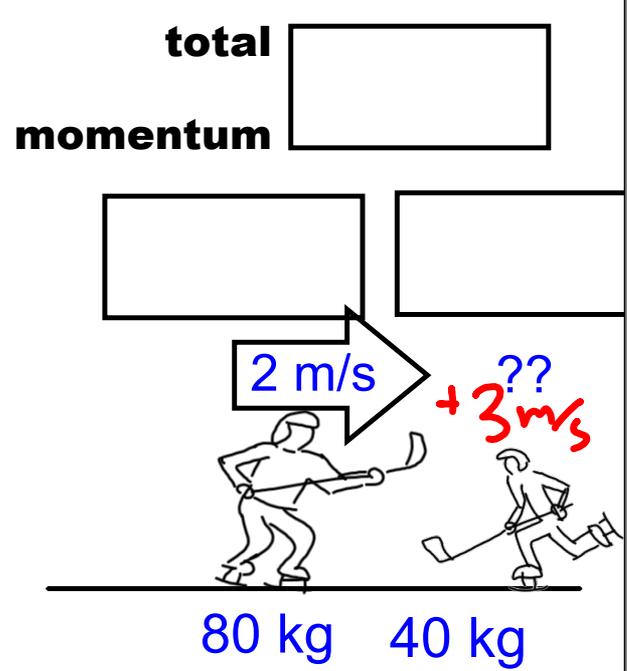
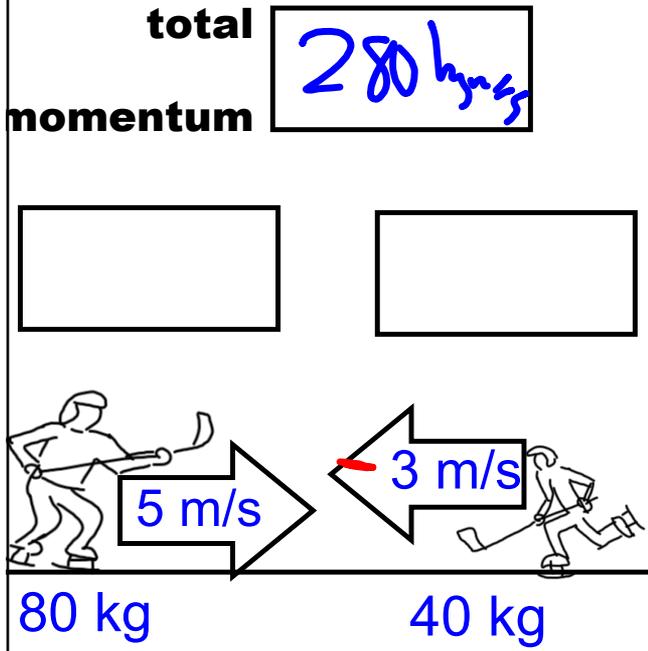
$160 \text{ kg}\cdot\text{m/s}$

80 kg                      40 kg

- 80                      - 80  
X = 160

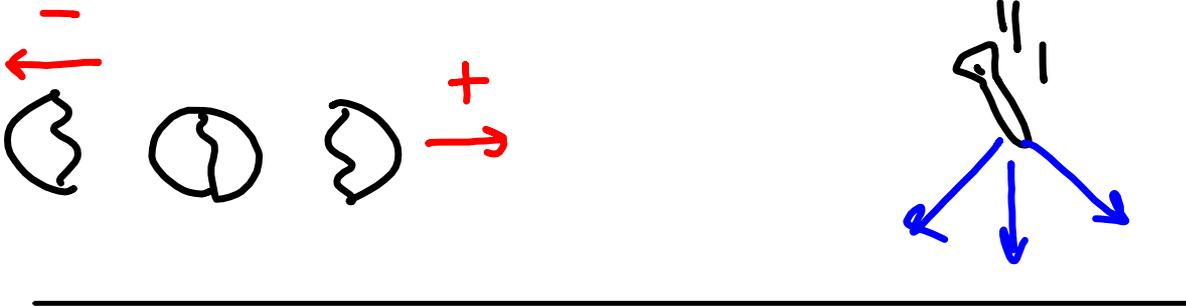
### Calculating Total Momentum Before a Collision

LEFT = NEGATIVE



Momentum never appears or disappears, it can only be transferred around by exerting impulses (force x time)

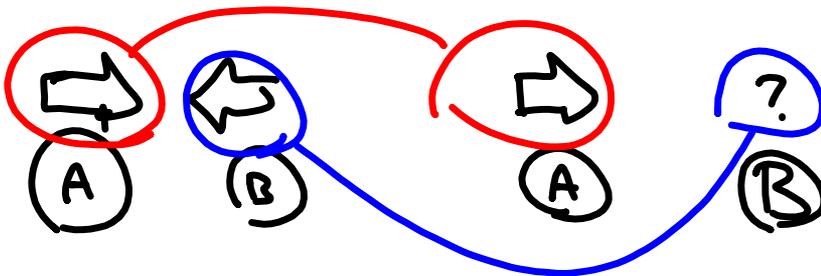
**Total Momentum is still there even after collisions and explosions**

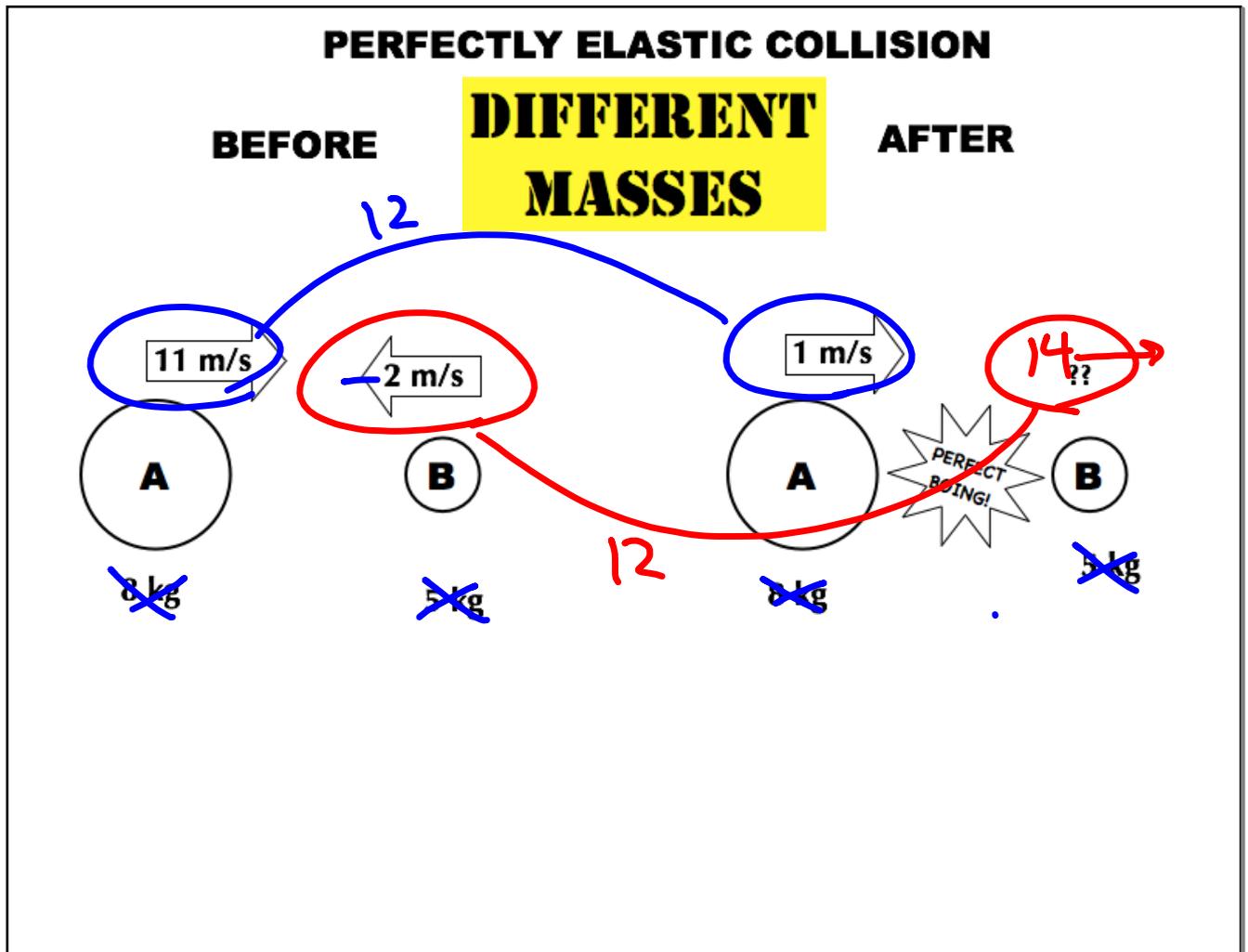


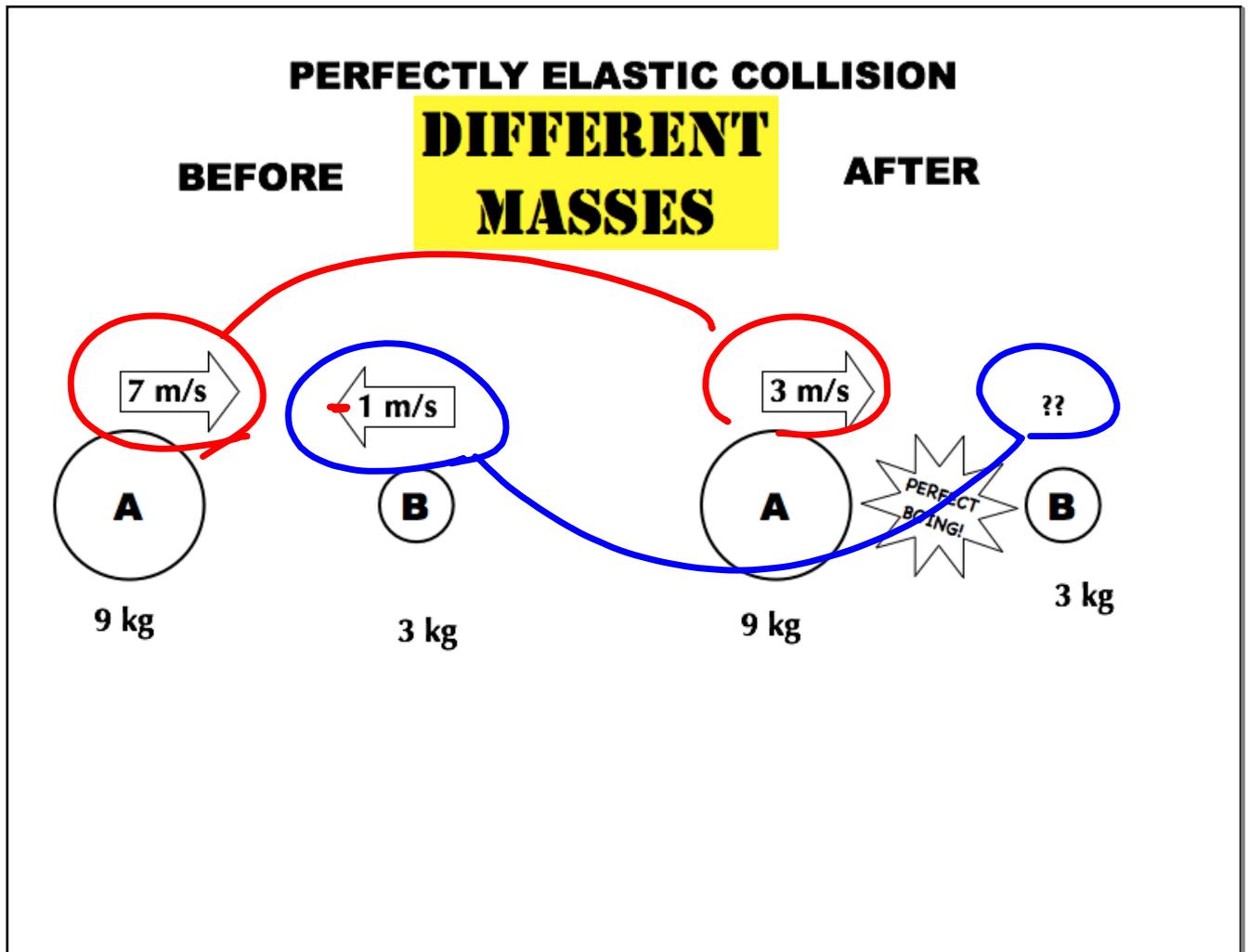
## PERFECTLY ELASTIC COLLISIONS

**Same mass >> VELOCITIES SWITCH!**

**Different masses >> ANOTHER TRICK!**







## **The Law of Conservation of Momentum**

**Total Momentum**  
**BEFORE a Collision** = **Total Momentum**  
**AFTER a Collision**

(If there are no outside forces)

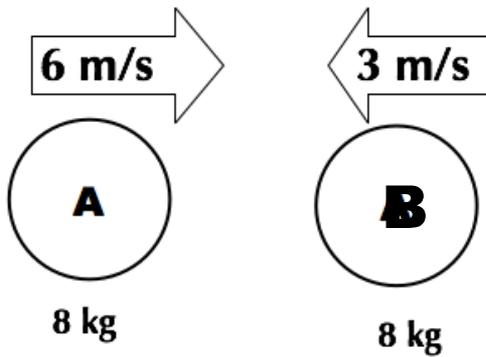
**What's wrong with this picture?**



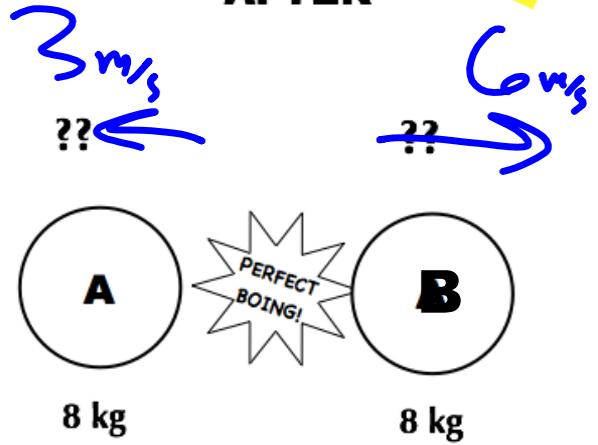
**PERFECTLY ELASTIC COLLISION**

**SAME  
MASSES**

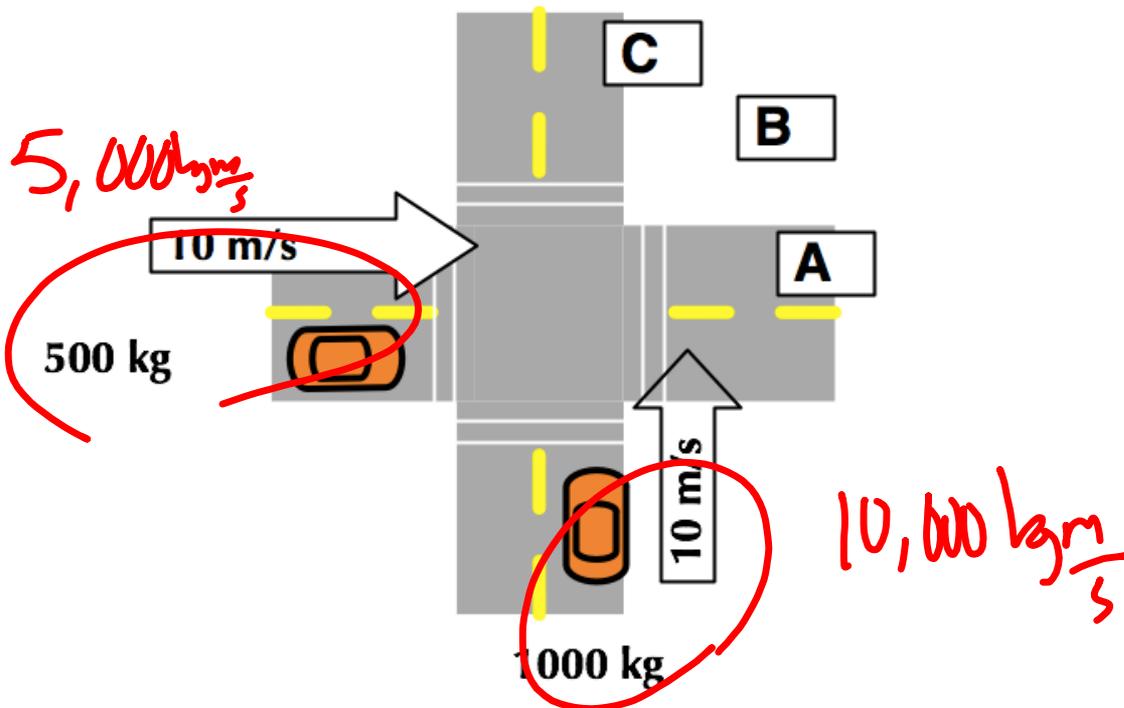
**BEFORE**



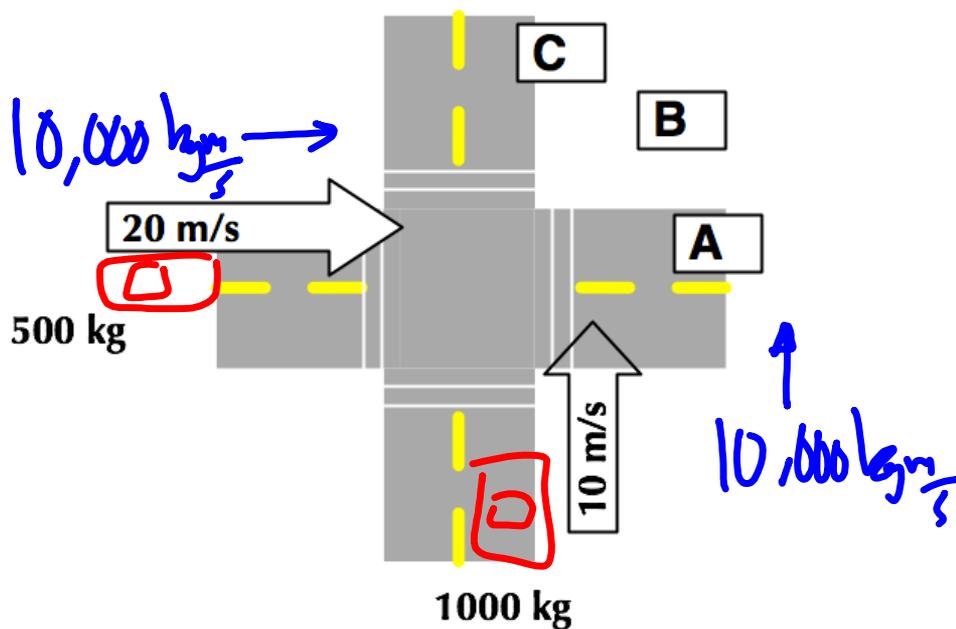
**AFTER**



Which way did the wreckage go after the collision?



### Totally Inelastic Collisions at an Angle



**Almost completely elastic collision; same mass.**

