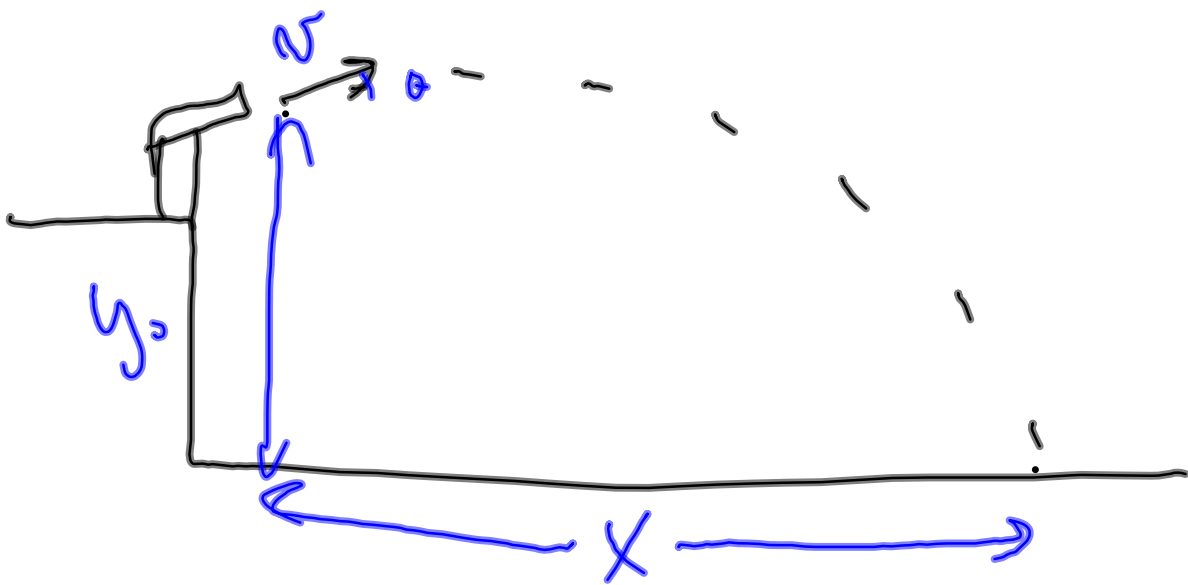


DRAG FORCES

- 1. PASCO Launcher Prediction**
- 2. Free Fall and Drag**
- 3. Coffee Filters - Lab**
- 4. Coffee Filters - Prediction**
- 5. From Forces to Motion: $F = kv^2$**
- 6. From Forces to Motion: $F = kv$**

1. PASCO Launcher Prediction



2. Free Fall and Drag

Drag depends on...

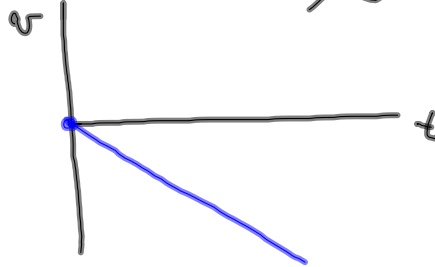
density / viscosity

relative v

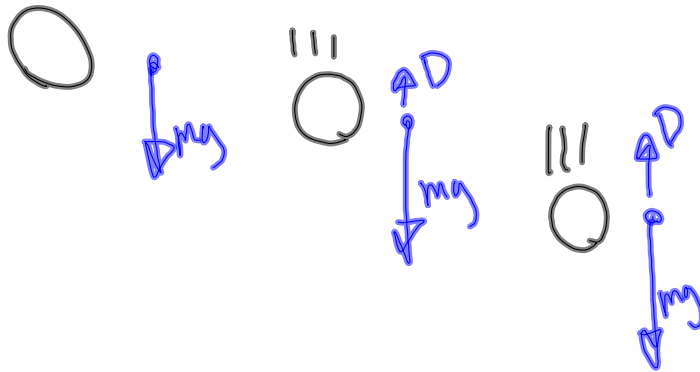
[shape
texture

cross-sectional area

Free fall
 $a = (-9.8 \text{ m/s}^2) \hat{j}$



not free fall

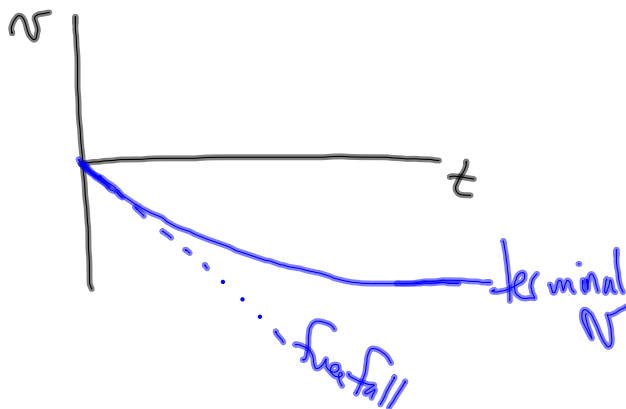


eventually...



$$\sum F = 0$$

$$D - mg = 0$$



We want to isolate the dependence of
drag forces on velocity

Drag depends on...

density / viscosity

shape

texture

cross-sectional area

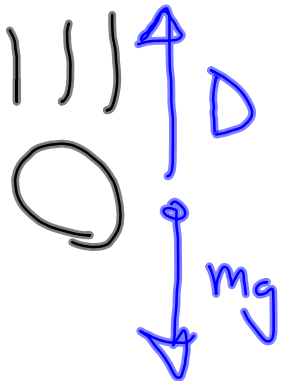
relative v

THOUGHT #1

→ hold constant

We want to isolate the dependence of drag forces on velocity

eventually...



$$\sum F = 0$$
$$D - mg = 0$$

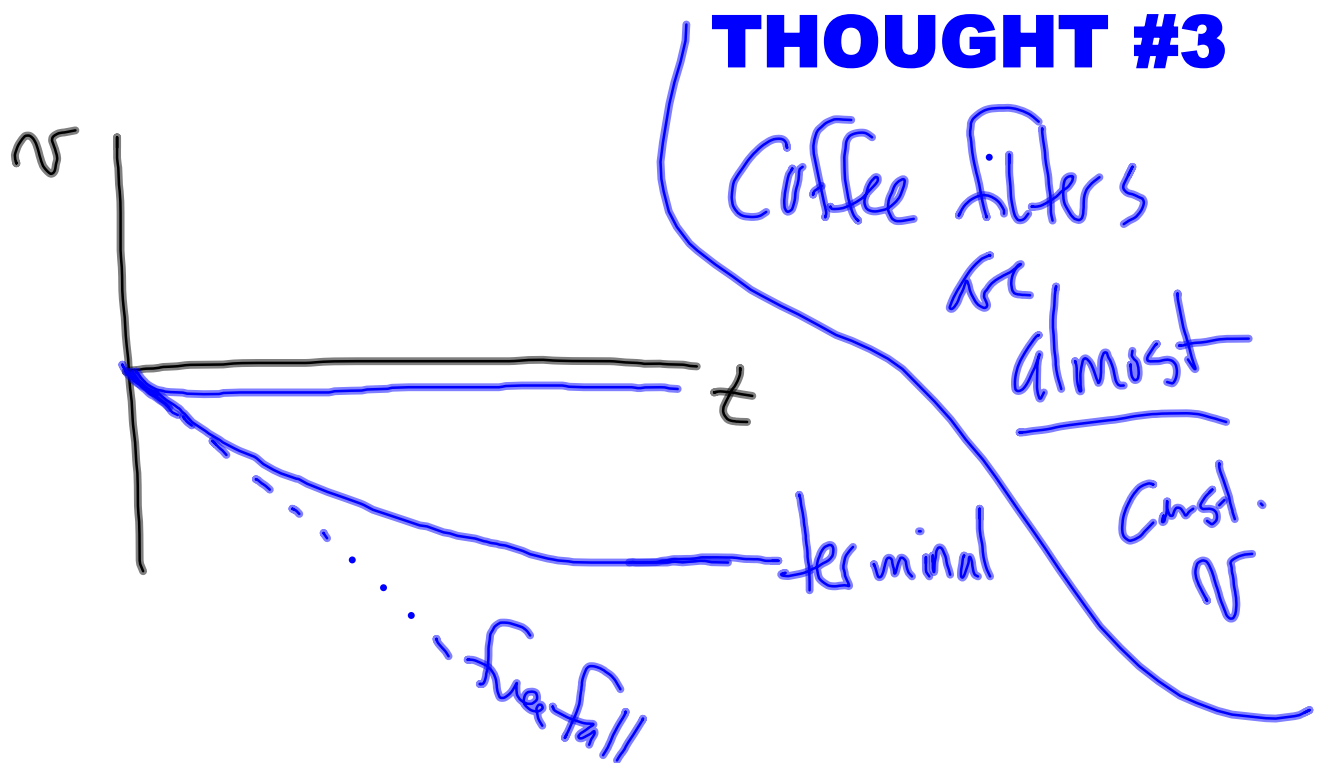
THOUGHT #2

at v_{terminal}

$$D = mg$$

mass of one coffee filter: 0.94 grams

We want to isolate the dependence of drag forces on velocity



3. Coffee Filters - Experiment

What is the relationship between drag force and velocity?

$$D = kv^n$$

(=mg)

v	F

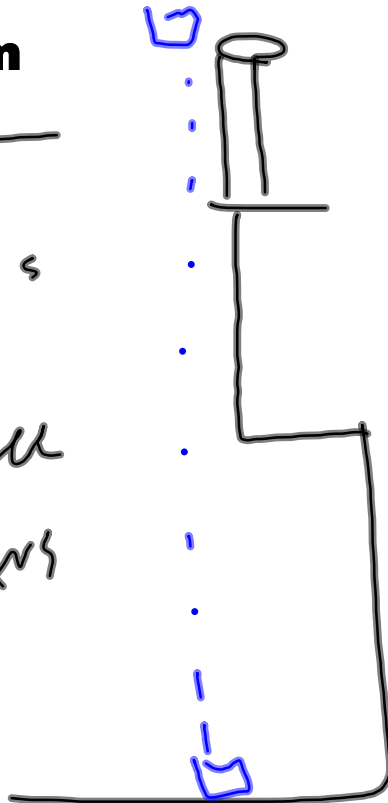
v ($= \frac{d}{t}$)

4. Coffee Filters - Prediction

$$y_0 = 4.55 \text{ m}$$

$$t = 2 \text{ s}$$

coffee filters



$$D = kv^n$$

5. From Forces to Motion: $F = kv^2$

$$D = kv^2$$

a lot
packed
in

at terminal v...

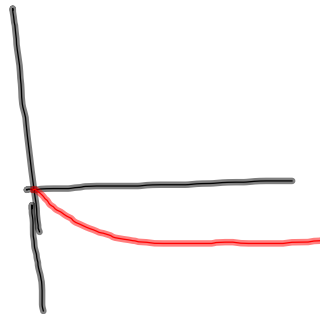
$$kv^2 - mg = 0$$

$$kv^2 = mg$$

$$v = \sqrt{\frac{mg}{k}}$$

$$\uparrow kv^2$$

$$\downarrow mg$$



$$D = kv$$

$$ma = kv$$

$$m \frac{dv}{dt} = kv$$



Antiderivative = Integration example

$$a = 3t - 2$$

$$v = \frac{3t^2}{2} - 2t + v_0$$

$$a = 3t - 2$$

$$\frac{dv}{dt} = 3t - 2$$

$$dv = 3t dt - 2 dt$$

$$\int_{v_0}^v dv = \int_0^t 3t dt - \int_0^t 2 dt$$

$$\left[v \right]_{v_0}^v = \left[\frac{3t^2}{2} \right]_0^t - \left[2t \right]_0^t$$

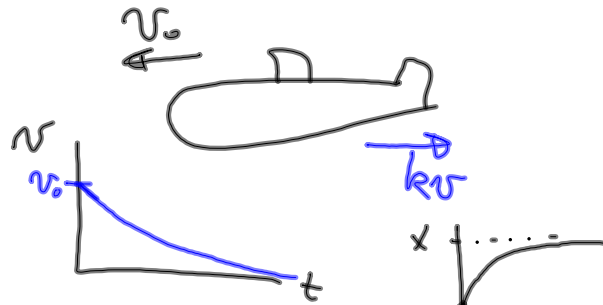
$$\left(v - v_0 \right) = \left[\frac{3t^2}{2} - \frac{3(0)^2}{2} \right] - \left[2t - 2(0) \right]$$

$$v - v_0 = \frac{3t^2}{2} - 2t$$

$$v = \frac{3t^2}{2} - 2t + v_0$$

6. From Forces to Motion: $D = kv$

$$D = kv \text{ (water)}$$



$$\sum F = ma$$

$$x = \frac{mv_0}{k} \left(1 - e^{-\frac{kt}{m}}\right)$$

$$-kv = ma$$

$$-kv = m \frac{dv}{dt}$$

constants

$$-kv dt = m dv$$

$$-\frac{k}{m} dt = \frac{dv}{v}$$

$$\int_0^t -\frac{k}{m} dt = \int_{v_0}^v \frac{dv}{v}$$

$$-\frac{k}{m} (t)_0^t = \left[\ln(v) \right]_{v_0}^v$$

$$-\frac{k}{m} (t-0) = \left[\ln(v) - \ln(v_0) \right]$$

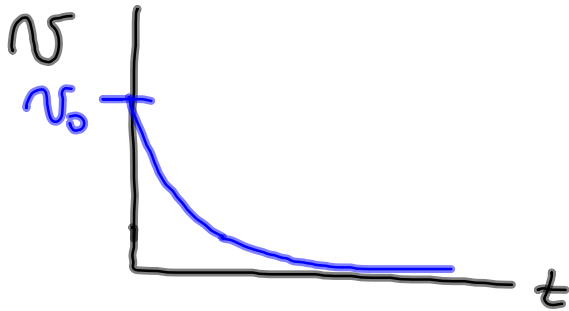
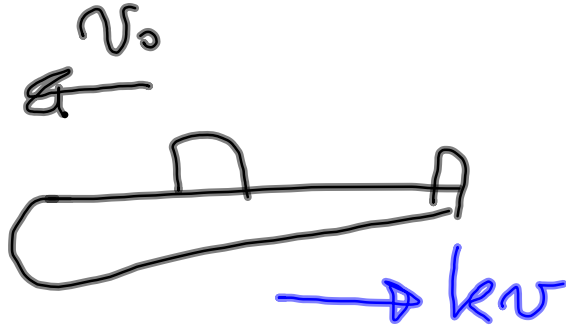
$$-\frac{k}{m} t = \ln(v) - \ln(v_0)$$

$$-\frac{k}{m} t = \ln\left(\frac{v}{v_0}\right)$$

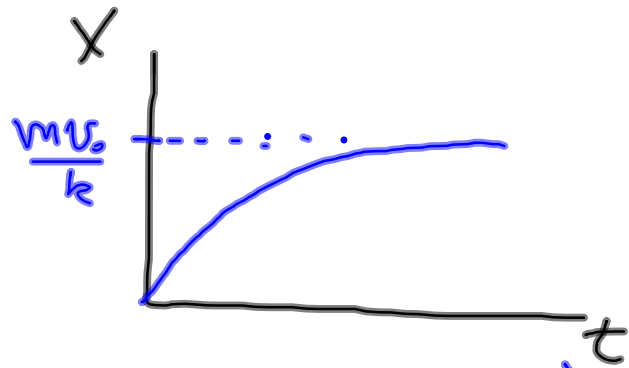
$$e^{-\frac{k}{m} t} = \frac{v}{v_0}$$

$$v = v_0 e^{-\frac{kt}{m}}$$

$$\frac{dx}{dt} = v_0 e^{-\frac{kt}{m}}$$

SUMMARY 1

$$v = v_0 e^{-\frac{k}{m}t}$$



$$x = \frac{mv_0}{k} \left(1 - e^{-\frac{k}{m}t} \right)$$

SUMMARY 2

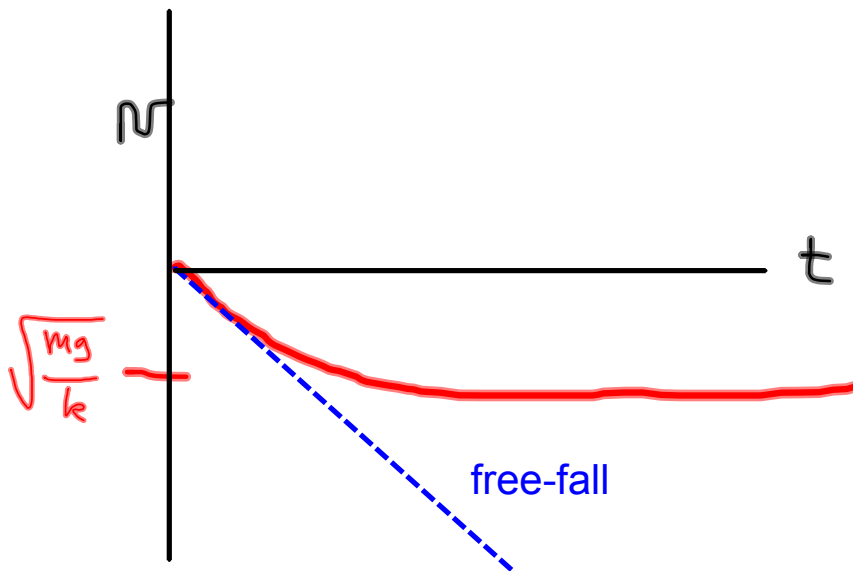
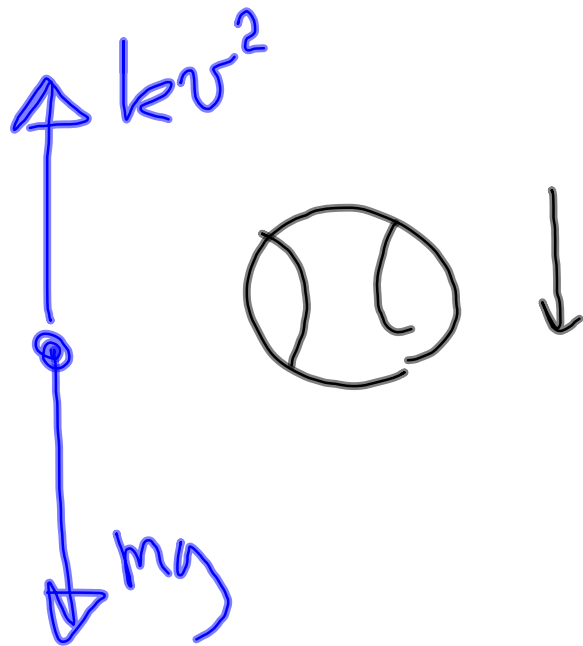
at terminal v ...

$$kv^2 - mg = 0$$

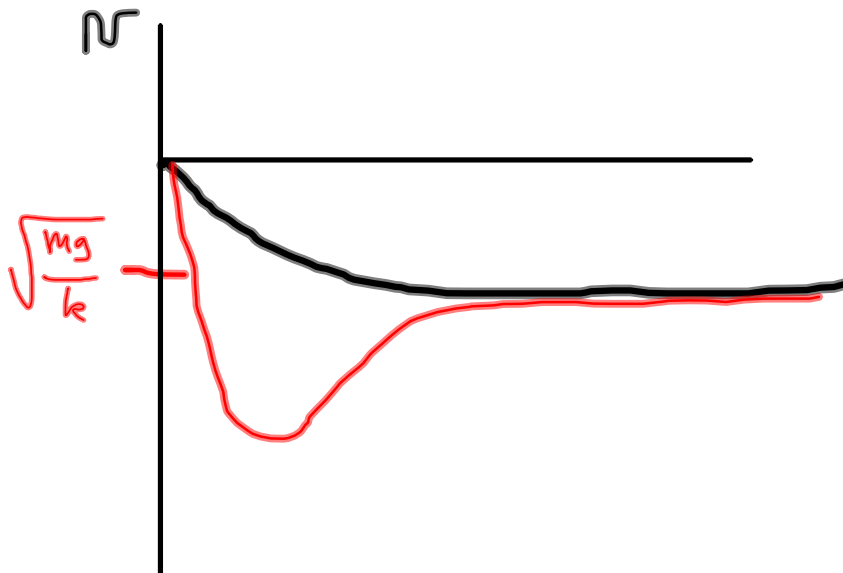
$$kv^2 = mg$$

$$v = \sqrt{\frac{mg}{k}}$$

terminal velocity for kv^2



What if something is propelled faster than its terminal velocity?



free-fall