

# Drag

Moving through a fluid, or a fluid moves past you.

~~Air resistance~~

~~Wind resistance~~

~~Air friction~~

The term "Drag"  
covers all of these.

Fluid = anything that flows (any gas or liquid)

Moving through a fluid, or a fluid moves past you.

Surfaces scraping over each other

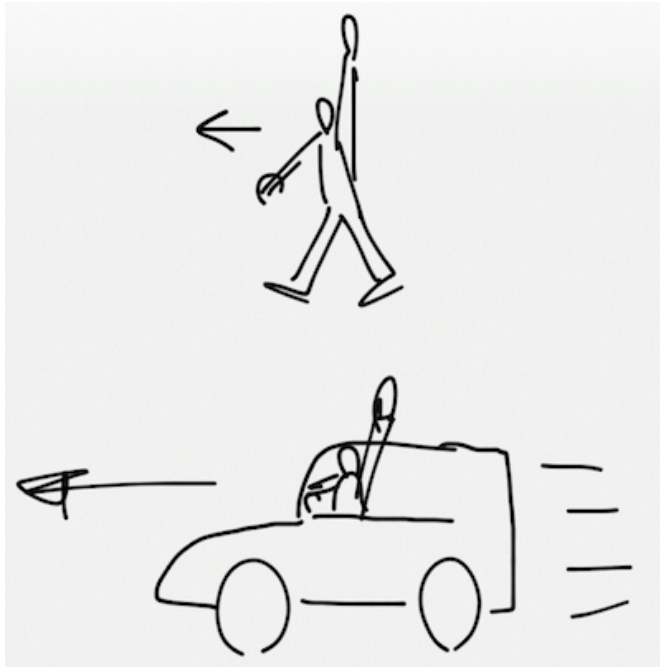
# Drag ~~=~~ Friction

Depends on

- ???

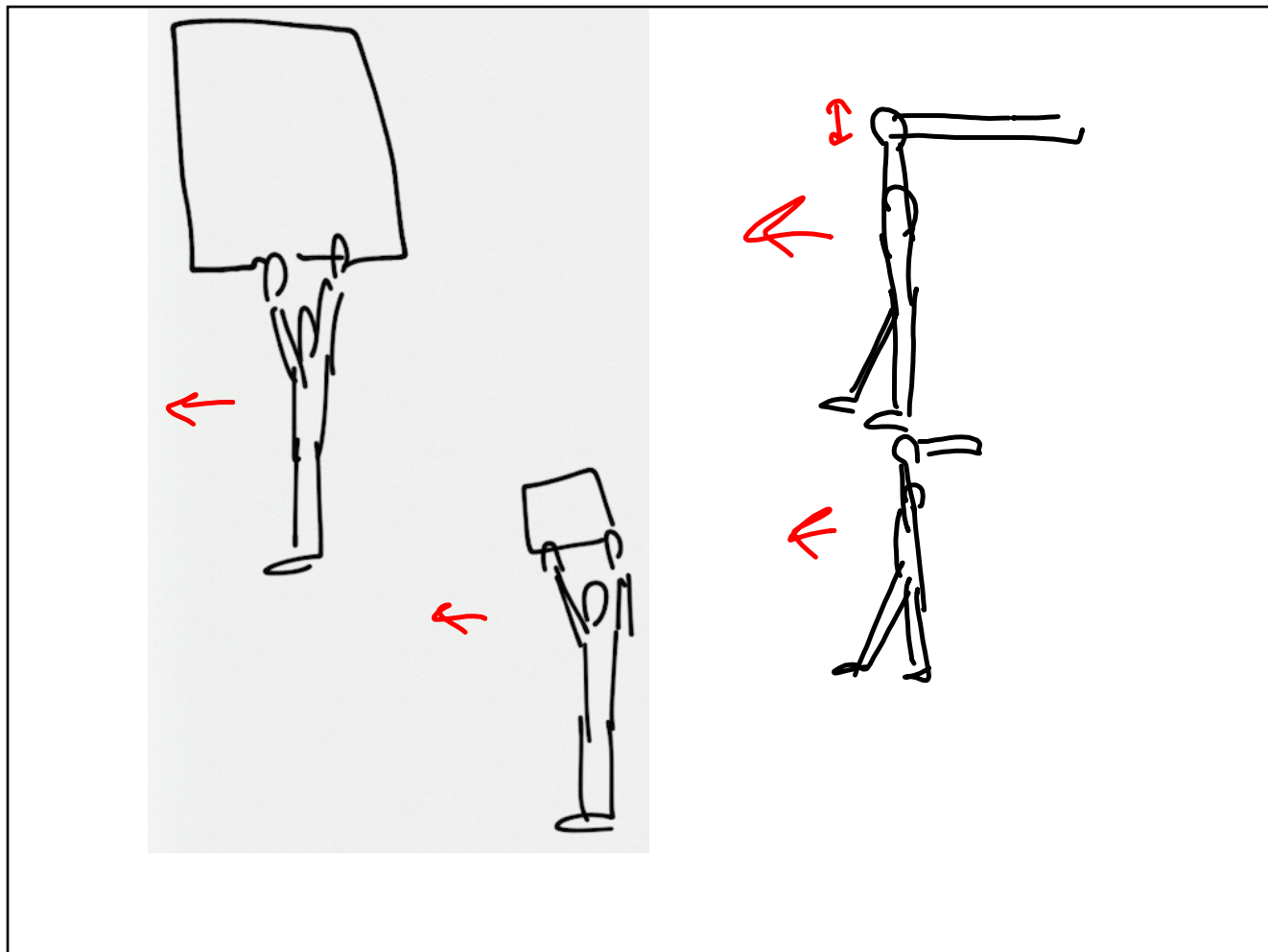
Depends on

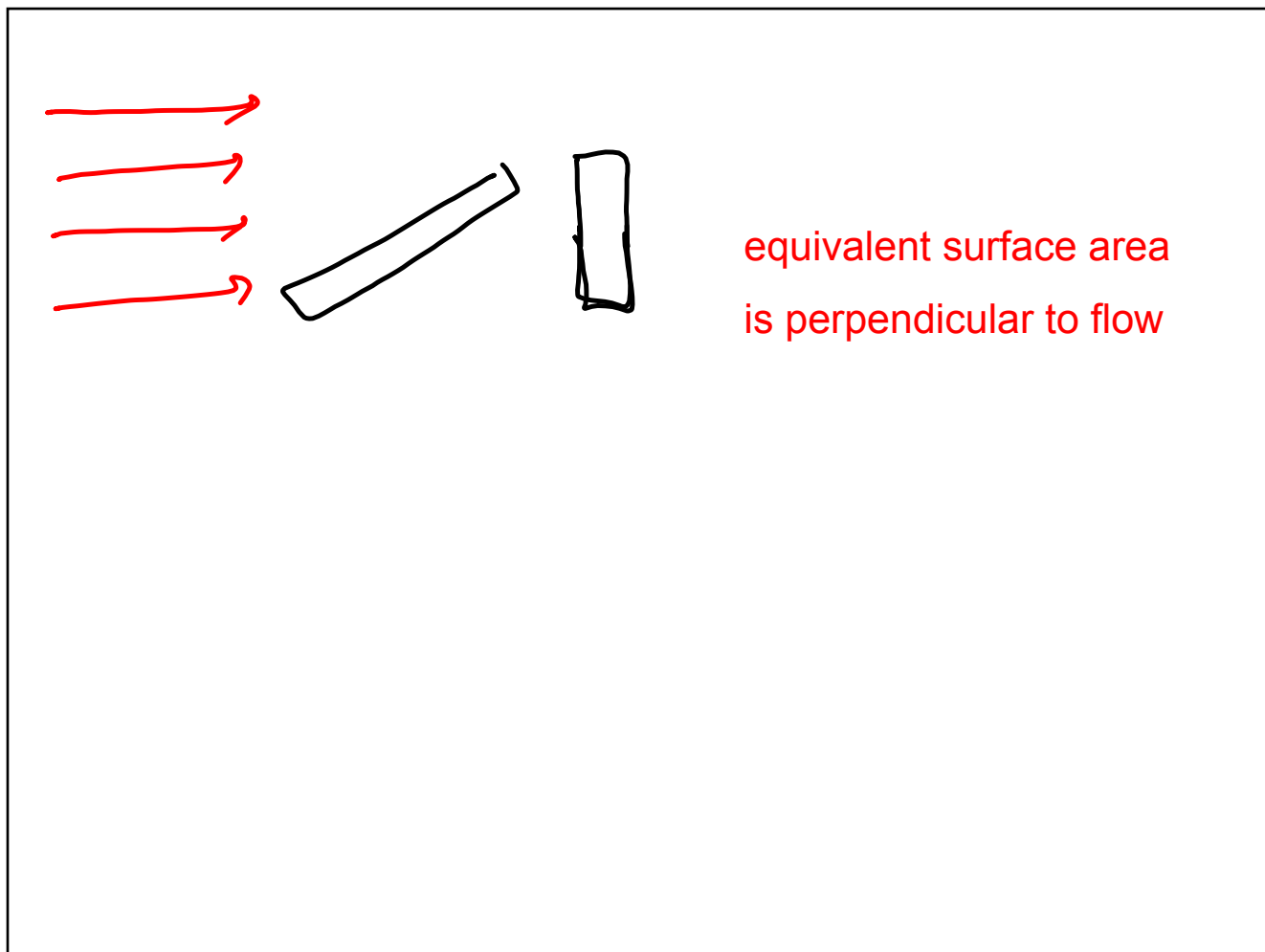
- The surfaces
- The force holding the surfaces together

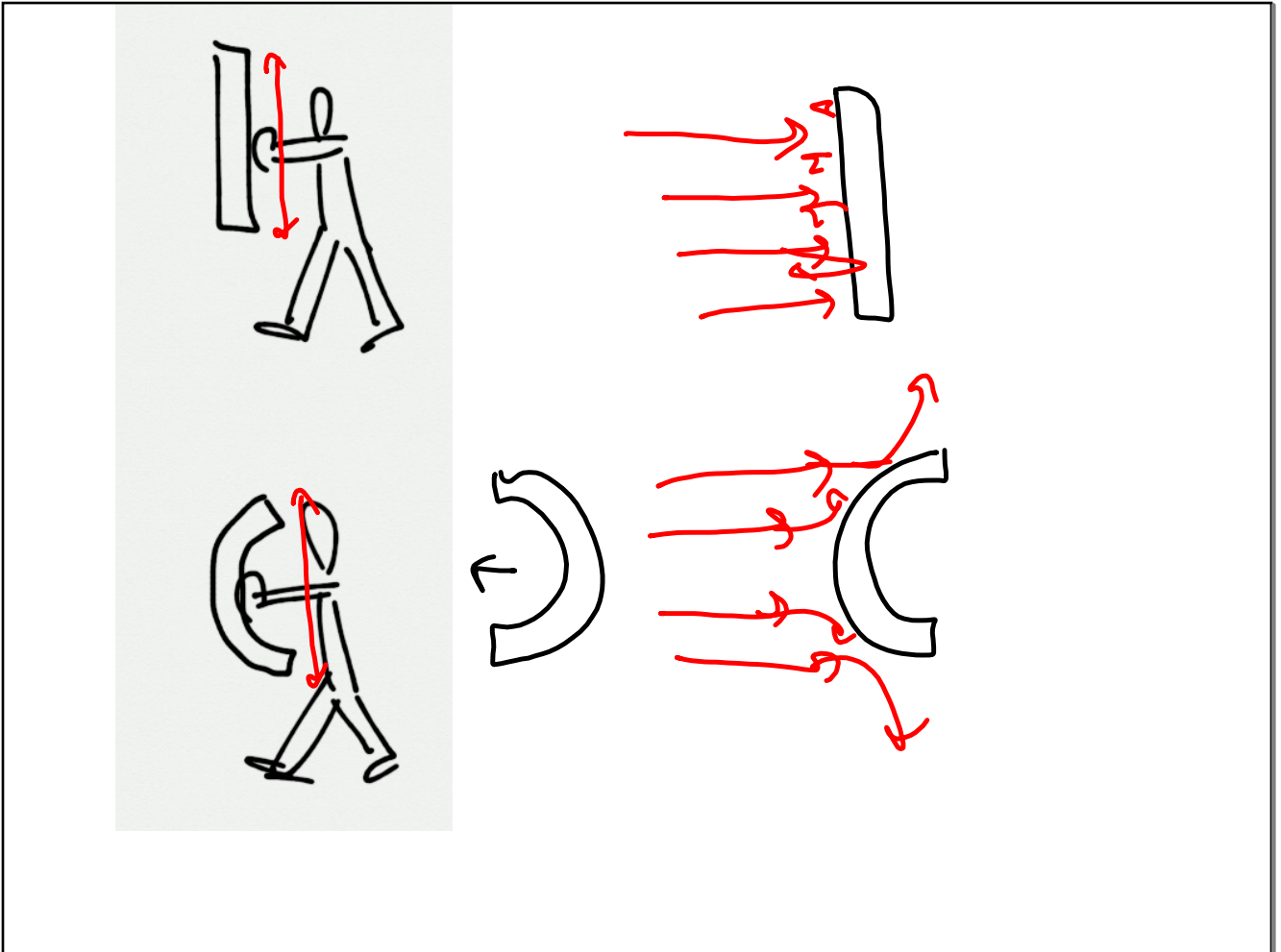


velocity  
~~speed~~

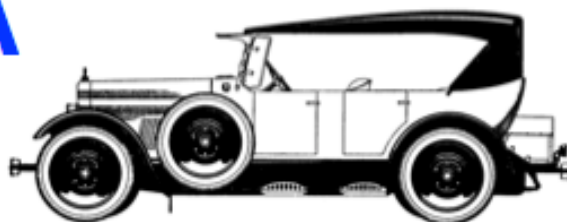
$D = \frac{v}{c}$





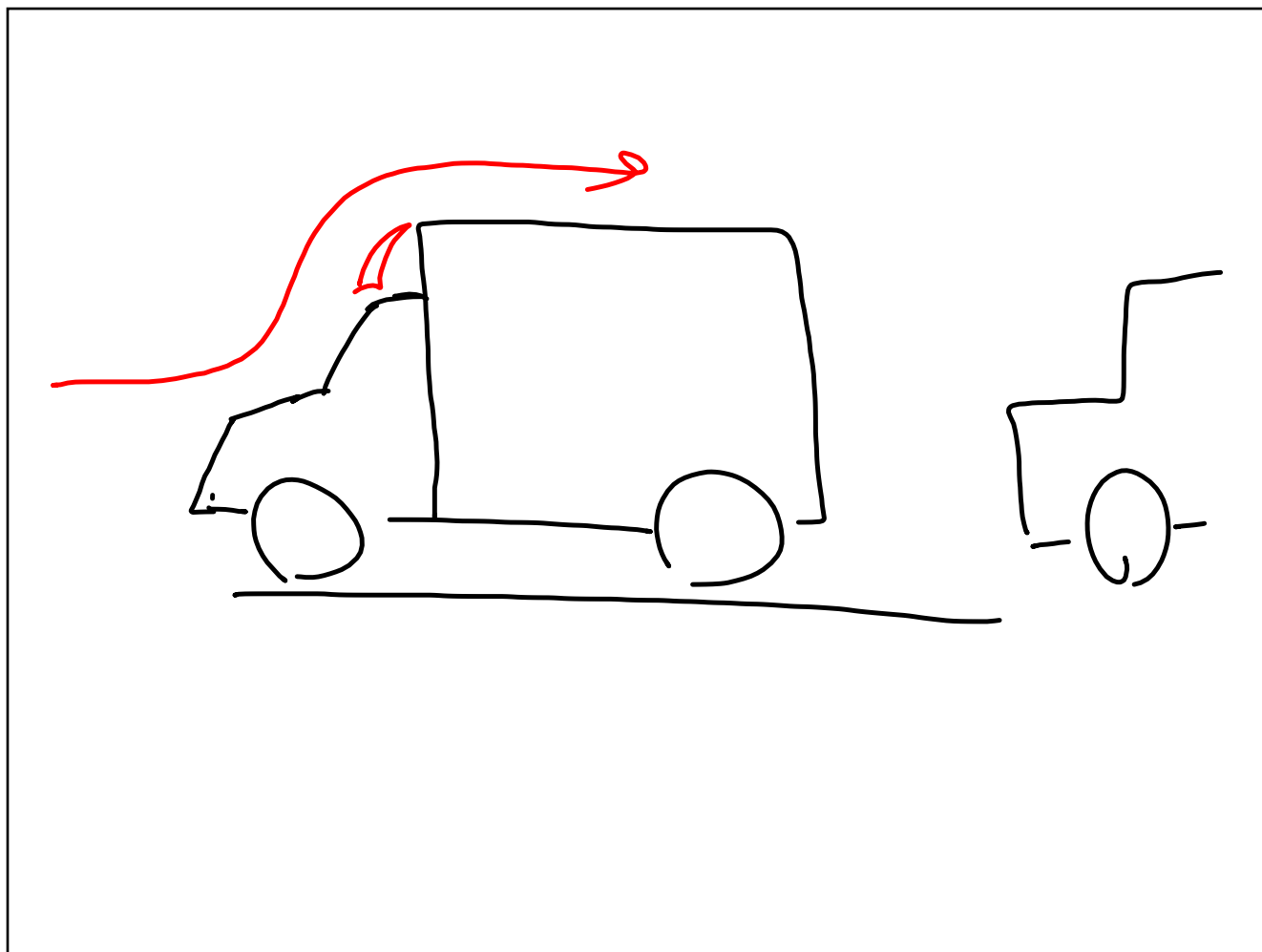


**A**



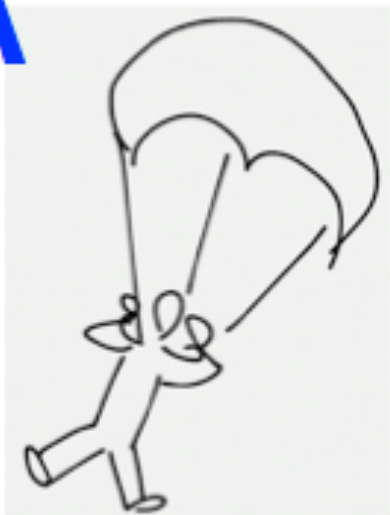
**B**







**A**



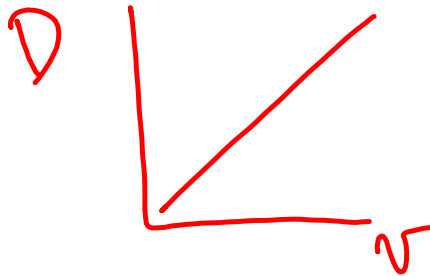
**B**



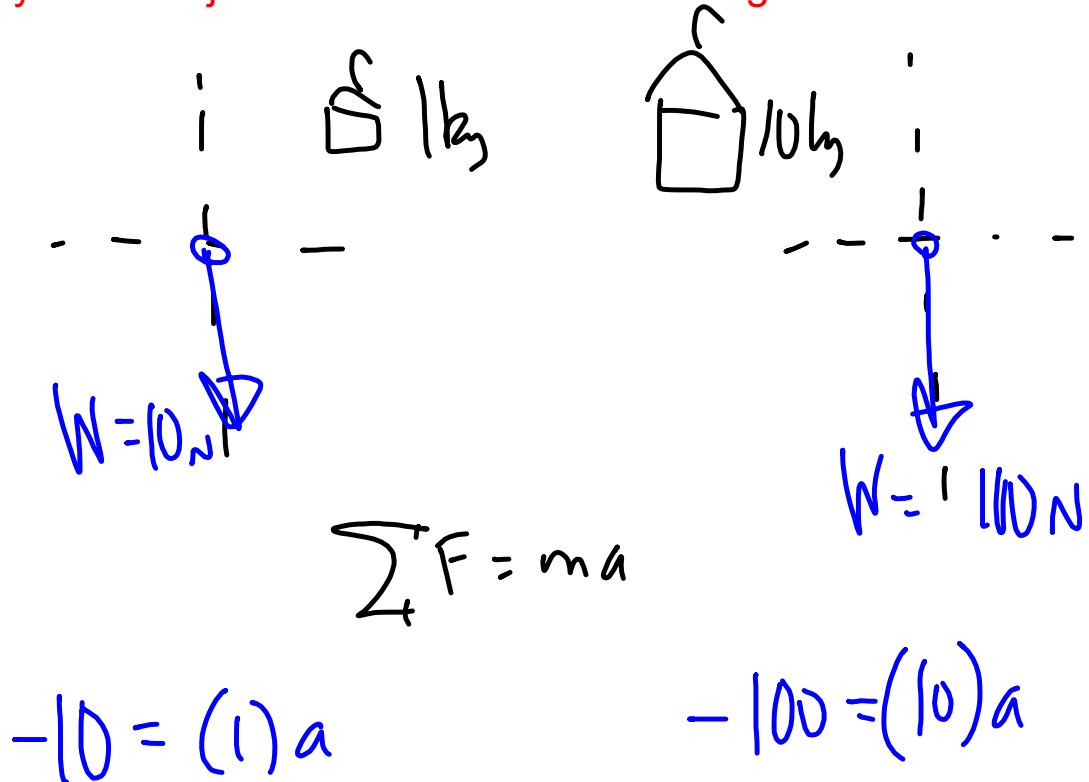
$$D = (\text{shape})(\text{surface } \perp)(\text{density velocity}) \sim v$$

$$D = -k v^n$$

$$D = -k v \quad \text{or} \quad -k v^2$$

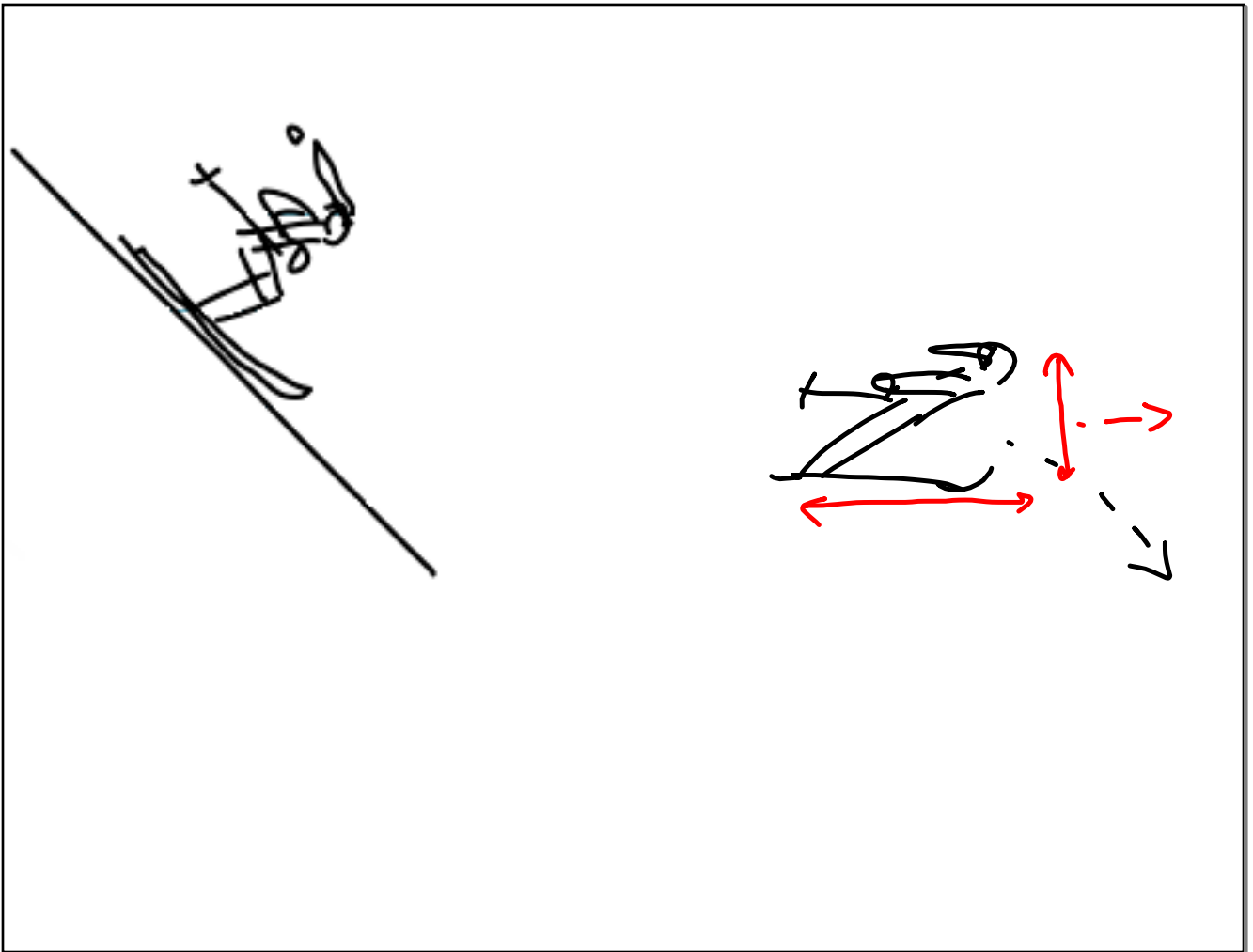


Why do all objects fall the same when Drag is not an issue?



With no drag, all things accelerate at 10 m/s/s downward, because -10 will always be the ratio of weight to mass.

Another way to think about it: heavier things get a stronger pull of gravity, but they also have more mass which makes them tougher to accelerate. The two effects cancel out.





## How do things fall when there is little or no drag ?

- a) They speed up.
- b) They slow down.
- c) They maintain constant speed.

# If there is drag - what happens to it as you fall?

Remember: faster means more drag.

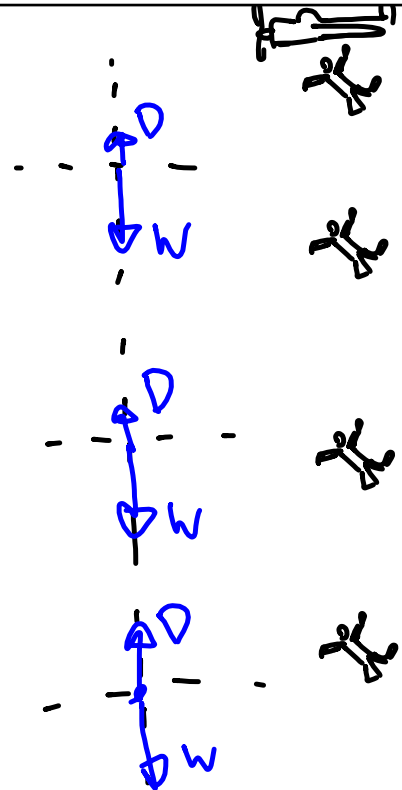
As you fall faster and faster,  
drag gets stronger and stronger.

When it equals the weight, you  
no longer accelerate.

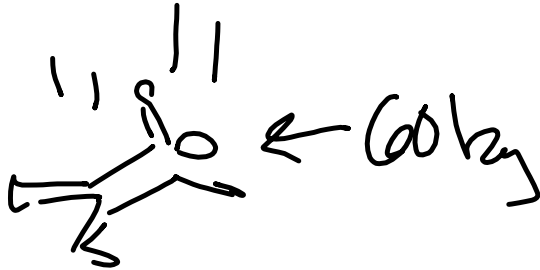
$$\sum F = 0$$

$$\therefore a = 0$$

The velocity you reached is now your  
terminal (ending) velocity.

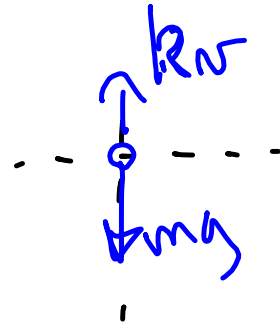
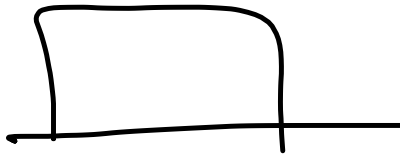


**Find his terminal velocity**



$$D = -kAv$$

$$k = 10$$



at term. vel.  $a = 0$

$$\therefore \sum_i F = 0$$

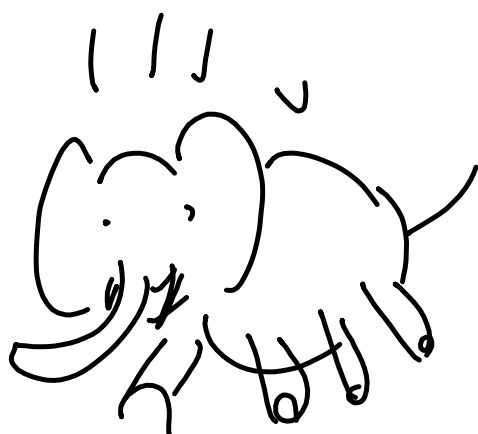
$$D - W = 0$$

$$kAv - mg = 0$$

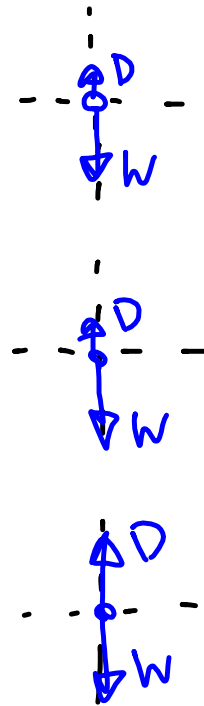
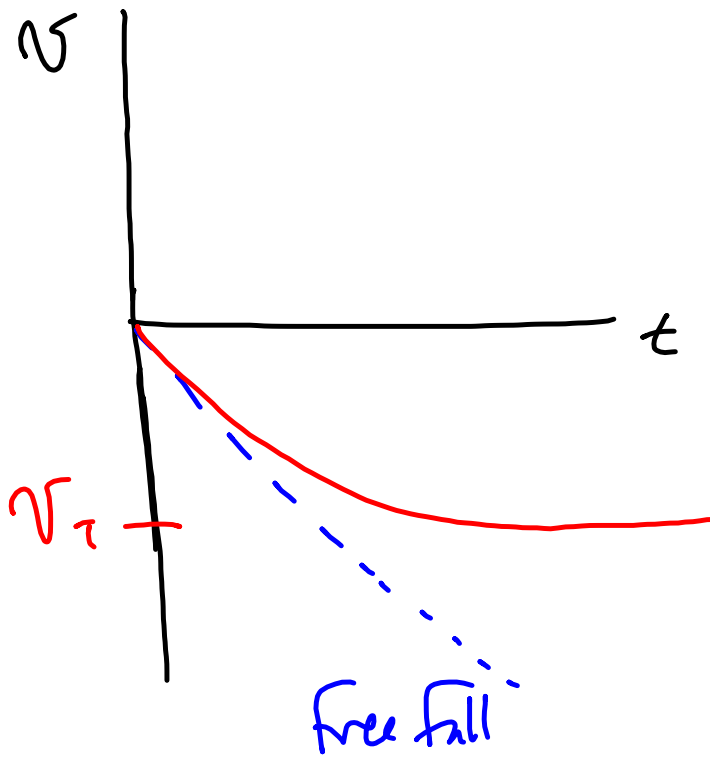
$$\begin{aligned} \therefore v &= \frac{mg}{k} = \frac{(60)(10)}{(10)} \\ &= 60 \frac{m}{s} \end{aligned}$$

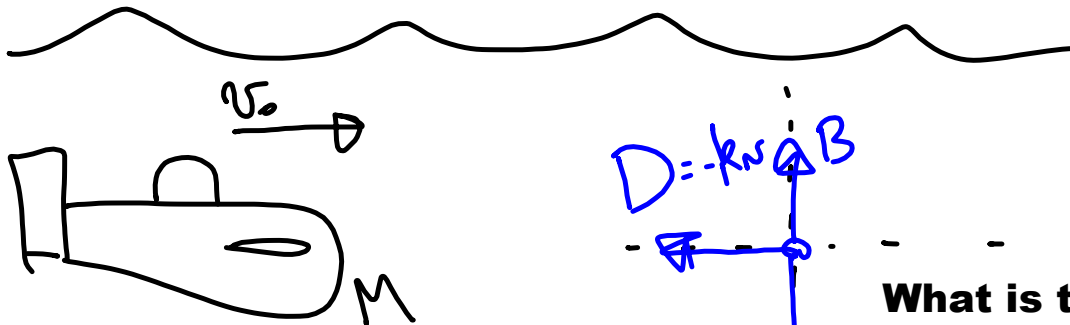


**Which one experiences more drag?**



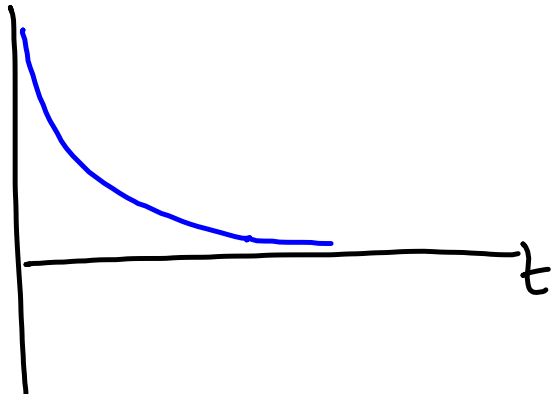
Falling from rest with drag.





$$D = -k v_0^2 B$$

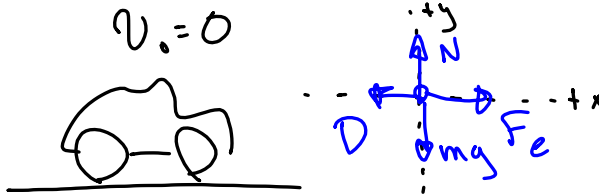
**What is the initial acceleration in terms of  $v_0$ ,  $M$ , and  $k$ ?**



$$\sum F_x = m a_x$$

$$-k v_0^2 = M a_x$$

$$-\frac{k v_0^2}{M} = a_x$$



The engine provides a constant force to the right of  $F_e$ . But there is also a drag force equal to  $-kv$ . The mass of the car is  $M$ .

a) Sketch the graph of the car's velocity over time.

b) What will the car's terminal velocity be? (In terms of  $k$ ,  $M$  and  $F_e$ .)

c) What was the initial accel?

$$\sum F = ma$$

$$F_e - kv = Ma$$

$$F_e = Ma$$

$$\frac{F_e}{M} = a$$

$$\sum F = ma$$

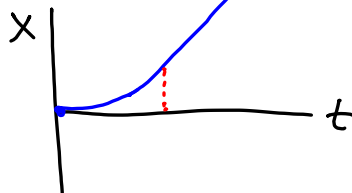
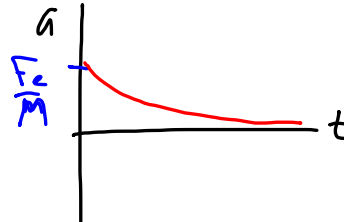
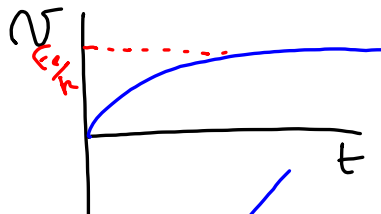
at term.  $v$ ,  $a = 0$

$$F_e - kv = 0$$

$$F_e = kv$$

$$\boxed{\frac{F_e}{k} = v}$$

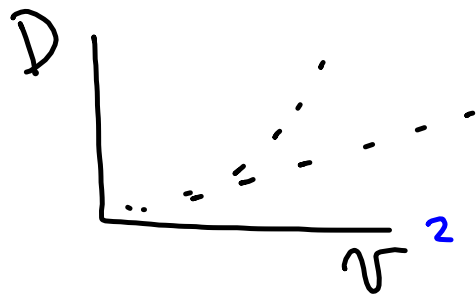
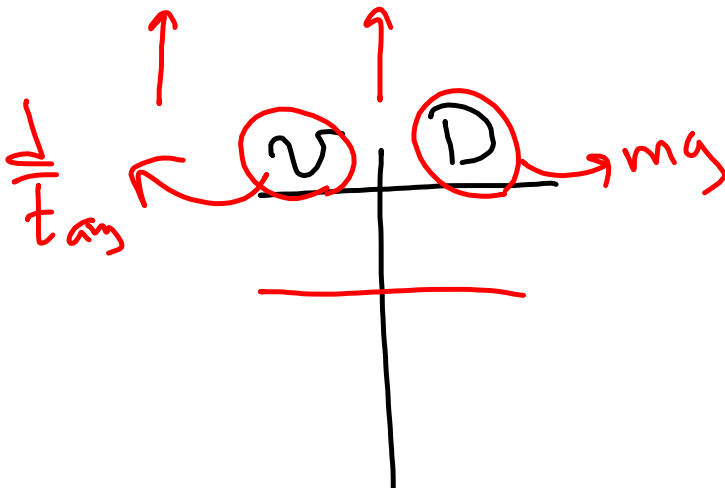
d) What does the accel vs. time graph look like?



**ACTIVITY : Find k for a coffee filter.**

**(Only checking calculations in excel & notebook.)**

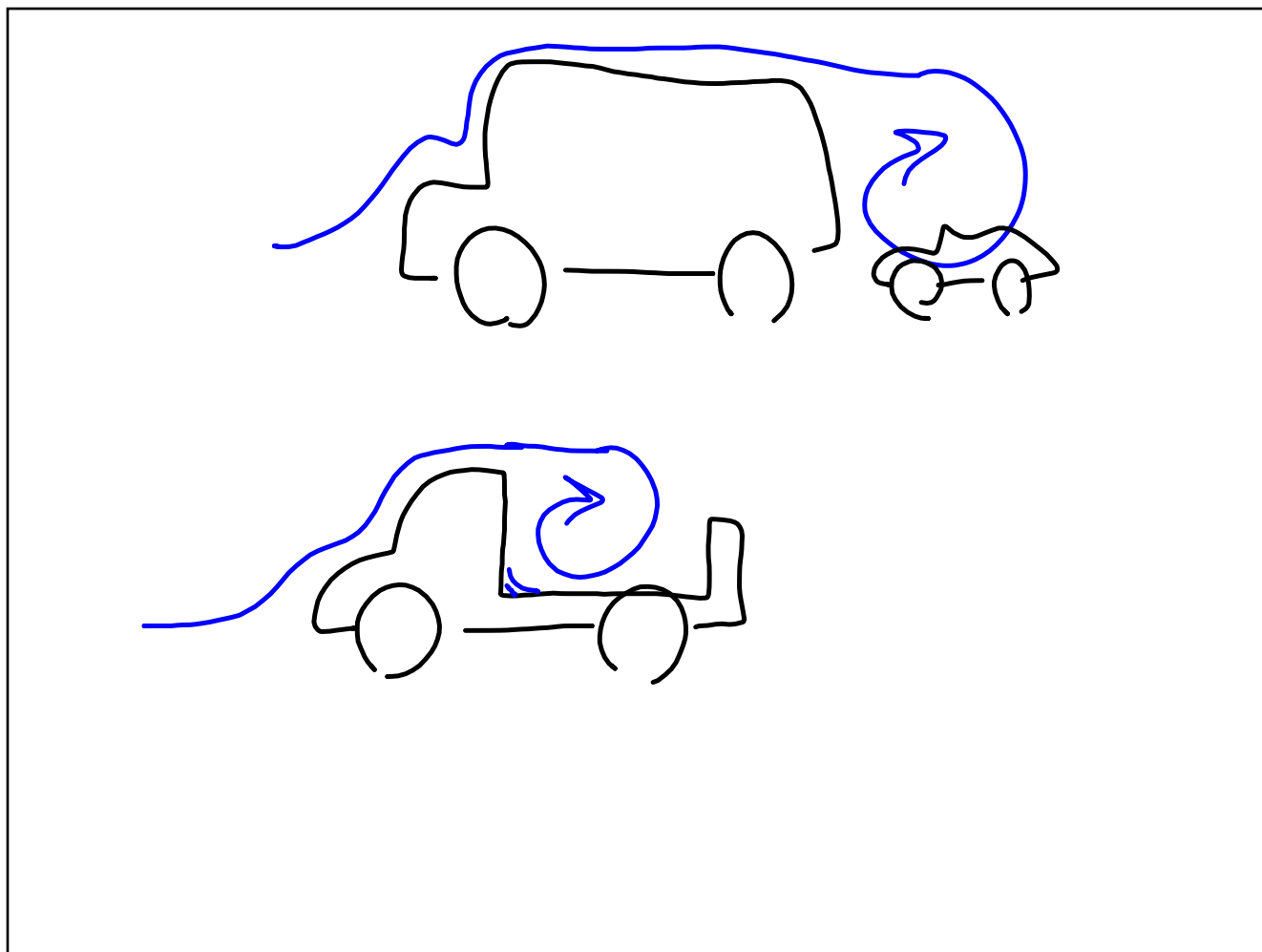
**$D = kv$  or  $-kv^2$**



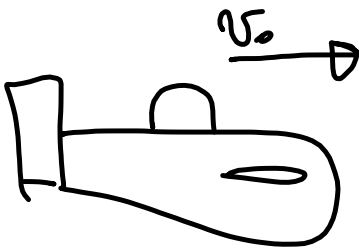
$$D = kv^2$$

$$y = 0.0055x$$

$$\therefore k = 0.0055 \text{ units??}$$

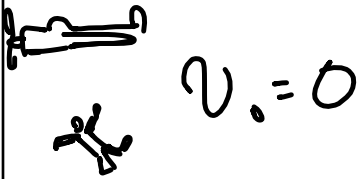


## Drag FR Typical Questions



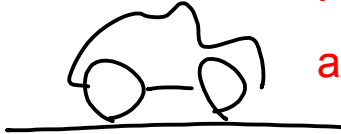
Only Drag acts  
with an initial  $v$

Initial accel?  
 $\sum_i F = ma$  ; plug in  $v_0$

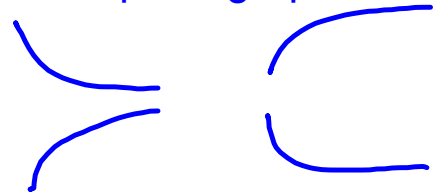


From rest, Drag builds  
against const. Force

Terminal  $v$ ?  
 $\sum_i F = ma$  ;  $a = 0$

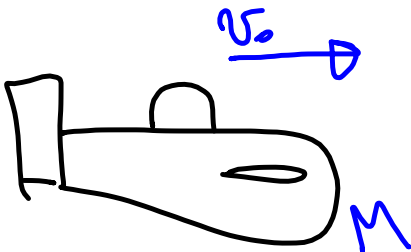


Shape of graphs?

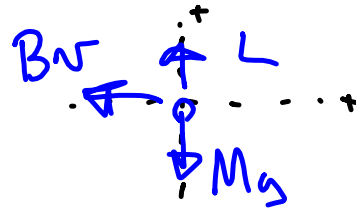


# Differential Equations, Part 1

## Setting up, but not solving



The submarine shuts off its engines and experiences a Drag force equal to  $-Bv$ .



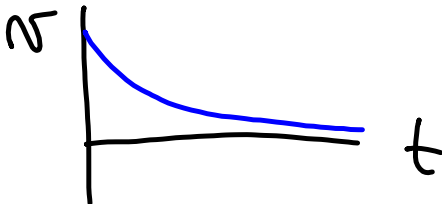
STEP 1: Write Newton's 2nd Law

$$\sum F = ma$$

STEP 2: Plug in the actual forces and actual variables

$$-Bv = Ma$$

STEP 3: Rewrite  $a$  as the derivative of  $v$



$$-Bv = M \left( \frac{dv}{dt} \right)$$

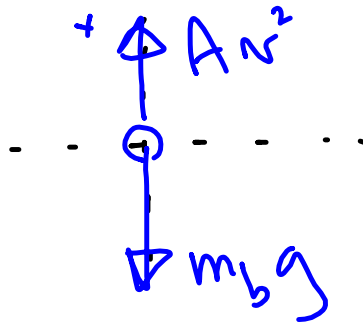


## Differential Equations, Part 1

### Setting up, but not solving

⑦  $v_0 = 0$   
 $m_b$

The ball falls from rest, and experiences a Drag force equal to  $-Av^2$ .



$$m_b g - Av^2 = -m_b \left( \frac{dv}{dt} \right)$$

